

# Abington Heights School District

## Calculus Curriculum



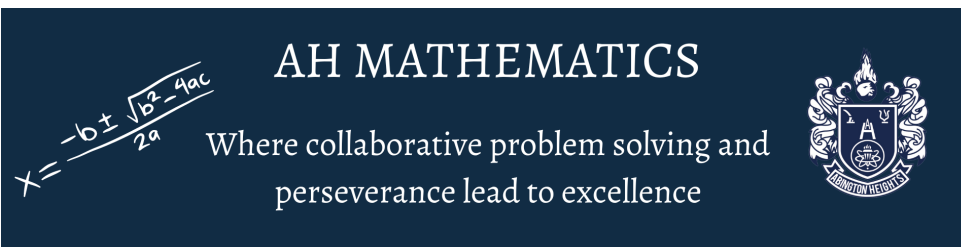
In Calculus, students develop their numeracy skills through the following areas of study:

1. Limits and Continuity
2. Derivatives
3. Applications of Derivatives
4. Analyzing Functions
5. Integrals

**Board Approval Date:** June 7, 2023

**Adoption:** 2023 - 2024 SY

**Review Date:**



# Abington Heights Math Framework

Stakeholders	Actions
<b>Students</b>	<ul style="list-style-type: none"> <li>★ Engage in mathematical discussions, share their ideas openly, be inquisitive, seek to understand and learn more about mathematical concepts, and try their best daily.</li> <li>★ Exhibit creativity and curiosity in problem solving individually and collaboratively.</li> <li>★ Persevere in engaging and challenging daily mathematical practice.</li> <li>★ Come prepared to learn every day.</li> </ul>
<b>Teachers</b>	<ul style="list-style-type: none"> <li>★ Create a safe and collaborative classroom environment where students feel vested in a shared vision for mathematical excellence.</li> <li>★ Develop high quality instruction that meets the needs of all learners through differentiation.</li> <li>★ Use a variety of 21st century methodologies to advance learning.</li> <li>★ Partner with parents and guardians to support student success.</li> <li>★ Establish a collaborative community within the building and amongst grade levels to ensure a cohesive level of instruction.</li> </ul>
<b>Building Leaders</b>	<ul style="list-style-type: none"> <li>★ Deeply understand the needs of teachers, students, the instructional materials being used, programs being implemented, and the expectations for state-level assessment scores <ul style="list-style-type: none"> <li>○ Knowledgeable about program and grade level standards</li> <li>○ Ensure consistent and equal access to high-quality instructional materials and resources, building.</li> </ul> </li> <li>★ Be partners with teachers, students and families: <ul style="list-style-type: none"> <li>○ Provide guidance and support to the mathematical community.</li> <li>○ Understand needs of teachers, students and families.</li> </ul> </li> <li>★ Trust the educators to make professional decisions based on program, student, and district needs.</li> </ul>
<b>Central Admin</b>	<ul style="list-style-type: none"> <li>★ Effectively communicate to the school board and community specific areas of need and how to support teachers and building leaders in a quest for mathematical excellence</li> <li>★ Deeply understand the needs of teachers, students, the instructional materials being used, programs being implemented, and the expectations for state-level assessment scores <ul style="list-style-type: none"> <li>○ Have a common metric for mathematical excellence.</li> <li>○ Ensure consistent and equal access to high-quality instructional materials and resources, district.</li> <li>○ Re-examine best practices/curriculum routinely (6 years).</li> </ul> </li> <li>★ Support a culture of collaboration between the other stakeholder groups to maintain the standard of excellence of the Abington Heights</li> <li>★ Trust the educators to make professional decisions based on program, student, and district needs.</li> </ul>
<b>Parents/Community</b>	<ul style="list-style-type: none"> <li>★ Be a strong support system and contribute by building a positive math community for students.</li> <li>★ Encourage a positive math mindset.</li> <li>★ Have conversations with their children about school and ask what they are learning about in school.</li> <li>★ Be open, receptive to the district's ideas about student learning and reach out to teachers/school to learn more about how they can support.</li> <li>★ Trust the educators to make professional decisions based on program, student, and district needs.</li> </ul>
<b>School Board</b>	<ul style="list-style-type: none"> <li>★ Provide the fiscal resources to support: <ul style="list-style-type: none"> <li>○ Highly qualified professionals for mathematics</li> <li>○ High-quality instructional materials</li> <li>○ Effective and efficient math interventions for remediation</li> <li>○ Professional development for math content and instructional practices</li> </ul> </li> <li>★ Trust the educators to make professional decisions based on program, student, and district needs.</li> </ul>

### Calculus Scope and Sequence

Month	Unit	Estimated Number of Weeks
September	Functions	2
September - October	Limits	2
October	Definition of Derivative	2
November - December	Derivative Rules	6
December - January	Implicit & Higher Order Differentiation	3
February	Related Rates	3
March	Logarithms & Logarithmic Differentiation	2
March	Optimization	2
April	Curve Sketching	3
April - May	Indefinite Integration	4
	Definite Integration & Mean Value Theorem	2
June	Final Exam Review	1

Unit	Essential Questions	Content	Skills	Activities	Assessment / Evidence of Learning
<b>Functions</b>	<p>What does the notation <math>f(x)</math> mean and how can it be manipulated?</p> <p>How are functions added, subtracted, multiplied, divided, and composed?</p>	Function manipulation	<p>Compose functions</p> <p>Factoring sum and difference of cubes</p> <p>Interpret function notation</p> <p>Utilize algebraic skills to add, subtract, multiply and divide functions</p>	<p>Function Manipulation Flip Chart 1 and 2</p> <p>Group Practice Set</p> <p>Class Discussions</p> <p>Homework sets</p>	<p>Group Practice Set</p> <p>Functions Quiz</p>
<b>Limits</b>	<p>What is a limit?</p> <p>How can limits be evaluated using a graph?</p> <p>How can limits be evaluated algebraically?</p>	<p>Graphical Evaluation of Limits</p> <p>Algebraic Evaluation of Limits</p>	<p>Simplifying complex fractions to evaluate a limit</p> <p>Simplifying radical expressions to evaluate a limit</p> <p>Substituting to evaluate a limit.</p> <p>Factoring rational expressions to evaluate a limit</p> <p>Analyzing a graph to determine limits</p> <p>Analyzing a graph to determine one-sided limits</p>	<p>Introduction to Limits Flip Chart</p> <p>Algebraic Evaluation of Limits Flip Chart</p> <p>Graphical Evaluation of Limits Flip Chart</p> <p>Limits WeBWork</p> <p>Class Discussions</p> <p>Homework sets</p>	<p>Limits WeBWork</p> <p>Limits Quiz</p>

Unit	Essential Questions	Content	Skills	Activities	Assessment / Evidence of Learning
<b>Definition of Derivative</b>	<p>What is a derivative?</p> <p>How can one determine a derivative?</p> <p>What is a derivative used for?</p> <p>What is a difference quotient? What does it represent and how is this connected to the idea of a derivative?</p> <p>Looking at a graph, what can reasonably be determined about the value of a derivative at a give x-value?</p>	<p>Algebraic definition of derivative</p> <p>Conceptual definition of derivative</p> <p>Power Rule</p> <p>Application of derivative</p> <p>Notation</p>	<p>Estimate the value of a derivative by inspecting a graph</p> <p>Algebraically calculate the value of a derivative</p> <p>Determine the derivative of a function using the limit of the difference quotient</p> <p>Determine an expression for the difference quotient of a given function</p> <p>Develop a foundational understanding of derivative notation and introductory facts</p>	<p>What is Calculus? Flip Chart</p> <p>Difference Quotient Flip Chart</p> <p>Definition of Derivative Flip Chart</p> <p>Basic Power Rule Flip Chart</p> <p>Class Discussions</p> <p>Homework sets</p>	<p>Definition of Derivative Quiz</p>
<b>Derivative Rules</b>	<p>What shortcuts exist for determining the derivative of a function?</p> <p>How can I determine which derivative rule applies to a function?</p> <p>What is the process for applying each of the derivative rules?</p>	<p>Power Rule</p> <p>Product Rule</p> <p>Chain Rule</p> <p>Quotient Rule</p> <p>Trig derivatives</p> <p>Exponential and natural logarithm derivatives</p>	<p>Identify functions that have a structure which enables the application of the power/product/chain/qu otient rule.</p> <p>Identify the derivative of trigonometric, logarithmic, and exponential function</p>	<p>Power Rule WeBWork</p> <p>Product Rule WeBWork</p> <p>Chain Rule WeBWork</p> <p>Class Discussions</p> <p>Homework sets</p>	<p>Power Rule Quiz</p> <p>Power Rule WeBWork</p> <p>Product Rule Quiz</p> <p>Product Rule WeBWork</p> <p>Chain Rule Quiz</p> <p>Chain Rule WeBWork</p>

Unit	Essential Questions	Content	Skills	Activities	Assessment / Evidence of Learning
<b>Derivative Rules (continued)</b>			<p>Apply the appropriate shortcut to determine the derivative of a function</p> <p>Algebraically identify and determine equivalent forms of a derivative</p>		
<b>Implicit &amp; Higher Order Differentiation</b>	<p>What is meant by higher order differentiation?</p> <p>What notation is involved in higher order differentiation?</p> <p>In what situations is implicit differentiation useful?</p> <p>What is the process required to implicitly differentiate a function?</p> <p>How does implicit differentiation connect to previously learned lessons?</p>	<p>Implicit Differentiation</p> <p>Higher Order Differentiation</p> <p>Notation for higher order derivatives</p> <p>Higher Order Implicit Differentiation</p>	<p>Determine a higher order derivative for a given function</p> <p>Identify problems for which implicit differentiation would be a useful technique</p> <p>Apply to the process of implicit differentiation to determine a derivative</p> <p>Apply the concepts of higher order differentiation to solve problems</p>	<p>Higher Order Differentiation Flip Chart</p> <p>Implicit Differentiation 1 Flip Chart</p> <p>Implicit Differentiation 2 Flip Chart</p> <p>Higher Order &amp; Implicit Differentiation WeBWork</p> <p>Class Discussions</p> <p>Homework sets</p>	<p>Higher Order &amp; Implicit Differentiation WeBWork</p> <p>Higher Order &amp; Implicit Differentiation Quiz</p>

Unit	Essential Questions	Content	Skills	Activities	Assessment / Evidence of Learning
<b>Related Rates</b>	<p>What formulas or equations can be used to model a given scenario?</p> <p>What is meant by the term “related rates”?</p> <p>How can we use derivatives to solve related rates problems?</p>	<p>Related Rates circle problems</p> <p>Related Rates square problems</p> <p>Related Rates triangle problems</p> <p>Related Rates cube problems</p> <p>Related Rates sphere problems</p> <p>Related Rates cone problems</p>	<p>Model a given circumstance algebraically</p> <p>Use algebraic skills to produce an equation in only one variable</p> <p>Identify and apply appropriate differentiation techniques based on the structure of an equation</p> <p>Solve an equation for a unknown value</p>	<p>Related Rates Intro Flip Chart</p> <p>Related Rates Circles &amp; Squares Flip Chart</p> <p>Related Rates Spheres &amp; Cubes Flip Chart</p> <p>Related Rates Triangles Flip Chart</p> <p>Related Rates Cones Flip Chart</p> <p>Related Rates WebWorks A and B</p> <p>Class discussions</p> <p>Homework sets</p>	<p>Related Rates WebWork A</p> <p>Related Rates Quiz A</p> <p>Related Rates WebWork B</p> <p>Related Rates Quiz B</p>
<b>Logarithmic Differentiation</b>	<p>How do you obtain the derivative of a term with a variable exponent?</p> <p>How can I use algebraic manipulation to simplify the process of logarithmic differentiation?</p>	<p>Logarithmic differentiation technique</p> <p>Properties of logarithms</p>	<p>Expand logarithmic expressions</p> <p>Condense logarithmic expression</p> <p>Convert between logarithmic and exponential form</p> <p>Apply the technique of logarithmic differentiation</p>	<p>Properties of Logarithms Flip Chart</p> <p>Logarithmic Differentiation Flip Chart</p> <p>Basic Logarithms WebWork</p> <p>Class Discussions</p> <p>Homework sets</p>	<p>Basic Logarithm WebWork</p> <p>Basic Logarithms Quiz</p> <p>Logarithmic Differentiation Quiz</p>

Unit	Essential Questions	Content	Skills	Activities	Assessment / Evidence of Learning
<b>Optimization</b>	<p>What does it mean to obtain an optimal value?</p> <p>How can I use calculus techniques to determine optimal values?</p> <p>What equation can I use to model a given circumstance?</p>	Optimization procedure	<p>Develop an expression to model a described circumstance</p> <p>Identify the correct differentiation technique for the expression</p> <p>Solve an equation for its zeroes</p>	<p>Optimization Flip Charts</p> <p>Optimization WeBWork A</p> <p>Optimization WeBWork B</p> <p>Class discussions</p> <p>Homework sets</p>	<p>Optimization Quiz A</p> <p>Optimization WeBWork A</p> <p>Optimization Quiz B</p> <p>Optimization WeBWork B</p>
<b>Curve Sketching</b>	<p>How can derivatives be used to sketch a curve?</p> <p>What is a critical value? How is it found?</p> <p>What are relative extrema and how are they found?</p> <p>What are inflection points and how are they found?</p> <p>What is concavity? How does it relate to derivatives?</p>	<p>Critical Values</p> <p>Absolute Maxima/Minima</p> <p>Relative Maxima/Minima</p> <p>Inflection Points</p> <p>Curve Sketching</p> <p>Curve Sketching on a restricted domain</p> <p>Concavity</p>	<p>Obtain critical values of a function</p> <p>Classify critical values and relative/absolute maxima or minima</p> <p>Identify inflection points</p> <p>Analyze the function to determine increasing and decreasing intervals both algebraically and graphically</p> <p>Interpret algebraic analysis of a function and produce a sketch of the curve</p>	<p>Curve Sketching Intro Flip Chart</p> <p>Max/ Min Flip Chart</p> <p>Increasing and Decreasing Intervals Flip Chart</p> <p>Inflection and Concavity Flip Chart</p> <p>Sketching Flip Chart</p> <p>Sketching on Closed Interval Flip Chart</p> <p>Increasing and Decreasing Intervals Activity</p> <p>Curve Sketching Activity</p>	<p>Curve Sketching Activity</p> <p>Curve Sketching WeBWork</p> <p>Curve Sketching Quiz</p>



Unit	Essential Questions	Content	Skills	Activities	Assessment / Evidence of Learning
<b>Curve Sketching (continued)</b>				Curve Sketching WeBWork  Class discussions  Homework sets	
<b>Integration</b>	What is integration?  What common applications does integration have?  What is indefinite integration?  What is definite integration?	Indefinite Integration  Definite Integration  Mean Value Theorem  Area Under a Curve  U -Substitution	Integrate polynomials, trigonometric, exponential, and logarithmic functions  Calculate the average value attained by a function over a given interval  Apply the techniques of definite integration to calculate the area under a curve  Apply the process of U-Substitution	Introduction to Integration Flip Chart  Indefinite Integration Flip Chart  Definite Integration Flip Chart  U-Substitution Flip Chart  Basic Integration WeBWork  U-Substitution WeBWork	Indefinite Integration Quiz  Definite Integration & MVT Quiz  Integration WeBWork  Basic Integration WeBWork  U Substitution WeBWork  Indefinite Integration Quiz  U -Substitution Quiz

## Portrait of an Abington Heights Mathematician



By the end of Calculus, students will:

Limits and Continuity	Derivatives	Applications of Derivatives	Analyzing Functions	Integrals
<ul style="list-style-type: none"> <li><input type="checkbox"/> Estimate limits from graphs and tables</li> <li><input type="checkbox"/> Evaluate limits by algebraic manipulation</li> <li><input type="checkbox"/> Analyze graphs to determine one-sided limits</li> </ul>	<ul style="list-style-type: none"> <li><input type="checkbox"/> Determine the derivative of a function using the limit of the difference quotient</li> <li><input type="checkbox"/> Find derivatives of functions using the product, quotient, power, and/or chain rules</li> <li><input type="checkbox"/> Evaluate the derivatives of trigonometric, exponential, and logarithmic functions</li> <li><input type="checkbox"/> Determine a higher order derivative for a given function</li> <li><input type="checkbox"/> Apply the process of implicit differentiation</li> </ul>	<ul style="list-style-type: none"> <li><input type="checkbox"/> Use derivatives to solve related rates problems</li> <li><input type="checkbox"/> Use calculus-methods to determine optimal values</li> <li><input type="checkbox"/> Solve real-life optimization problems</li> </ul>	<ul style="list-style-type: none"> <li><input type="checkbox"/> Use derivatives to sketch a curve by obtaining critical values of a function, classifying as relative or absolute minima/maxima, identifying inflection points, and analyzing function to determine increasing and decreasing intervals</li> </ul>	<ul style="list-style-type: none"> <li><input type="checkbox"/> Integrate polynomials, trigonometric, exponential, and logarithmic functions</li> <li><input type="checkbox"/> Investigate properties of indefinite and definite integration</li> <li><input type="checkbox"/> Integrate with U-substitution</li> </ul>